Knowledge Organiser-Years 9-11

Year	Unit Title	Formula and key facts	Content Overview	Linked topics				
		Factor trees	Calculations, checking, rounding and	Core skill, lots of links.				
	Error! Reference	Significant figures	estimation					
	source not found.	Truncation	Factors, Multiples and Primes					
		Error intervals	Operations with Negative Numbers					
	Error! Reference	Simplifying and collecting like terms	Expression, equation, formula and identity	Core skill, lots of links.				
	source not found.	Expanding and factorising	Substitution					
			Multiplying single, double and triple					
			brackets					
			Linear and quadratic factorisation					
			Rearranging formulae					
	Error! Reference	Improper fractions	Four Operations with Fractions	Core skill, lots of links.				
	source not found.	Common denominators when adding and	Recurring decimals <-> Fractions					
		subtracting						
9		Cross cancelling when multiplying						
		Multiplying by reciprocal when dividing						
		Formal proof for recurring decimals to fractions						
	Y9 Test 1							
	Error! Reference	Sum of interior angles in a polygon = (number of	Angles in parallel lines	Algebra – 9.2				
	source not found.	sides -2) x 180	Interior/Exterior angle sums in polygons					
		Sum of exterior angles = 360						
		Interior angle + exterior angle = 180						
	Error! Reference	Simplifying and combining two ratios	Using Ratios to solve complex problems	Algebra – 9.2				
	source not found.		Simple proportion problems	Fractions – 9.3				
	Error! Reference	Circumference = πd or $2\pi r$	Area and Perimeter of all GCSE shapes	Ratio – 9.5				
	source not found.	Area = πr^2	Arc Length and Sector Area					
		Area/Arc length of a sector = Angle/360 x						
		area/circumference						

Error! Reference	√a x √b = √ab	Multiplication and Simplification	Number properties – 9.1	
source not found.	$\frac{\sqrt{a}}{\sqrt{b}} = \sqrt{\frac{a}{b}}$			
Error! Reference source not found.	$a^{2} + b^{2} = hyp^{2}$ $a^{2} = hyp^{2} - b^{2}$ $a \qquad b$	Pythagoras' Theorem in 2D and 3D	Algebra – 9.2 Perimeter and area – 9.6 Surds – 9.7	
	Y9 Te	est 2		
Error! Reference source not found.	Mean = $\frac{\Sigma f x}{\Sigma f}$ Position of median = (n+1)/2	Mean Mode Median Range Mean from frequency tables (grouped) Finding the mean given other totals	Calculations – 9.1 Algebra – 9.2	
9.10 Representing and interpreting data	Bar chart – gaps between bars and labels Pie chart – angle = $\frac{frequency}{total frequency} X 360$ Frequency polygon – plot points at the midpoint of the interval and connect with straight lines	Dual/Composite Bar Charts Stem and Leaf Pie Charts Line Graphs Frequency Polygons	Averages and range – 9.	
Error! Reference source not found.	Maintain equality Elimination method Substitution method	Solving equations including fractions Solving simultaneous equations by elimination and substitution.	Algebra – 9.2 Fractions – 9.3	
Error! Reference source not found.	SOHCAHTOA SOH Sin $\theta = \frac{Opposite}{Hypotenuse}$ Hypotenuse θ Opposite θ CAH $\cos \theta = \frac{Adjacent}{Hypotenuse}$ TOA $Tan \theta = \frac{Opposite}{Adjacent}$ Bearings – three digits, clockwise from North	Finding missing sides and angles using sohcahtoa. Bearings, including trigonometric problems Scale drawing	Ratio – 9.5 Perimeter and area – 9.6 Surds – 9.7 Pythagoras – 9.8	
	Y9 E>			
Error! Reference source not found.	Correlation or Relationship Extrapolation or interpolation	Including drawing and interpreting a line of best fit.	Representing data – 9.10	

	Error! Reference source not found.	Y=mx + c where m is the gradient and c is the y intercept Parallel – same gradient Perpendicular – $m_1 = -\frac{1}{m_1}$	Equation of a straight line Parallel and perpendicular lines.	Algebra – 9.2 Fractions – 9.3 Ratio and proportion – 9.5
	Error! Reference source not found.	Gradient represents the change in y for every unit increase in x	Interpretation of gradient using context	Linear graphs – 9.14
	Error! Reference source not found.	"n" is the position nth term is the formula to find term n Linear or quadratic	Linear and quadratic sequences	Algebra – 9.2
	Error! Reference source not found.	Finding a percentage Increasing/decreasing by a percentage Working backwards to find an original value Compound/simple interest	Multipliers Reverse Percentages Compound and Simple interest	Fractions and decimals – 9.3 Ratio and proportion – 9.5 Perimeter and area – 9.6
10	Error! Reference source not found.• $x^0 = 1$ • $x^n \div x^m = x^{n-m}$ • $x^{-n} - \frac{1}{2}$ • $(x^n)^m = x^{n \cdot m}$		Negative and Fractional Indices Index laws Standard form Calculating with standard form (calc and non-calc)	Calculations (with decimals) – 9.1 Fractions – 9.3 Surds – 9.7
		Standard form - a x 10 ^b where 1≤a<10 and b must be an integer		
		Y10 Test 1		
	Error! Reference source not found.	$\frac{a}{\sqrt{b}}$ by multiplying both the numerator and the denominator by \sqrt{b} $\frac{a}{\sqrt{b}\pm c}$ by multiplying both the numerator and the denominator by the conjugate of $\sqrt{b}\pm c$	Multiplying linear combinations of surds Rationalising the denominator, including use of conjugate.	Algebra (expanding brackets) – 9.2 Fractions – 9.3 Surds – 9.7

Error! Reference source not found.	Sphere Cylinder Cone Share $A\pi r^2$ V= 4/3 πr^3 SA = $2\pi r^2 + 2\pi rh$ V = πr^2h SA = $\pi rl + \pi r^2$ V = Rectangular Prism Triangular Prism SA = $2(lw+lh+wh)$ V = lwh SA = $bh + 2ls + lb$ V = $1/2(bl)h$ Volume of Pyramid = $\frac{1}{3}$ base area × height	Surface area and volume of 3D Shapes	Perimeter, area, circles – 9.6 Pythagoras – 9.8
Error! Reference source not found.	For: $ax^2 + bx + c = 0, x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$	Solving by Factorisation Solving using the Quadratic Formula	Algebra – 9.3 Surds – 9.7
Error! Reference source not found.	 Information required: Transformation with vector Rotation with angle, direction if applic and centre Reflection with equation of the line of reflection Enlargement with scale factor and cent 		Fractions – 9.3 Ratio – 9.5 Graphs and coordinates – 9.14
Error! Reference source not found.	Relative Frequency = $\frac{Observed Occurences}{Total trials}$ Estimated occurrences = Probability x number trials	Probability of single events	Fractions – 9.3 Ratio – 9.5
Error! Reference source not found.	Direct proportion in form y=kt Indirect proportion in for xy=k	Simple direct/inverse proportion. Algebraic Proportion. Y10 Exam	Algebra – 9.3 Ratio – 9.5
Error! Reference source not found.	$A = \frac{1}{2}absinC$ $\frac{Sin A}{a} = \frac{Sin B}{b} = \frac{Sin C}{c}$	Sine, Cosine and Area Rule $A = \frac{1}{2}absinC$	Angles – 9.4 Area and perimeter – 9.6

	$\frac{a}{Sin A} = \frac{b}{Sin B} = \frac{c}{Sin C}$		Trigonometry (including bearings) – 9.12	
	$a^2 = b^2 + c^2 - 2bcCos A$		5.12	
Error! Reference	Area SF = Linear scale $factor^2$	Scale factors for conversion between	Ratio and proportion – 9.5	
source not found.	Volume SF = <i>Linear scale factor</i> ³	lengths, areas and volumes.	Area and perimeter – 9.6 Pythagoras (for problem solving) – 9.8 Percentages (multipliers) – 10.2 3D shapes (SA and V) – 10.5	
Error! Reference source not found.	https://www.youtube.com/watch?v=2oudsyluB8Y	Constructions with straight edge and compass. Solving loci problems through construction and scale drawing.	3D shapes (properties) – 10.5	
Error! Reference	Cumulative Frequency – plot cumulative frequency		Ratio and proportion – 9.5	
source not found.	values at the end of the interval and join up with lines or a smooth curve passing through all the points. Histograms – area of the bar is the frequency, plot frequency density where: $FD = \frac{Frequency}{Class width}$		Area – 9.6	
Error! Reference	To estimate the speed on a curved distance time	Drawing and interpreting graphs	Area – 9.6	
source not found.	graph, draw a tangent and find its gradient To find the distance travelled on a speed time graph calculate or estimate, if curved, the area under the graph.	Calculating gradient and area under graphs. Estimating gradient and area under graphs.	Linear graphs – 9.14	
	Y10 Test 2			
Error! Reference	• Angle in a semi-circle is 90°	Learn circle theorems and language to use	Angles – 9.4	
source not found.	 Angles subtended from the same arc at the circumference are equal The radius meets a tangent at 90° 	to describe them.	Algebra (forming equation – 9.2 Trigonometry (problem solving) – 10.10	

	Error! Reference	 The angle at the centre is double the angle at the circumference Alternate Segment theorem Distances from a point to where the tangents meet the circle are equal If a radius bisects a chord, it is perpendicular If a radius is perpendicular to a chord, it also bisects it Look out for isosceles triangles with two radii as sides 		Algebra – 9.3
	source not found.	 reverses the inequality sign. For quadratic inequalities: Find critical values by finding roots Use a graph or number line to determine inequality solution. 		Linear graphs – 9.14 Quadratics – 10.6
	Error! Reference source not found.	$Speed = \frac{Distance}{Time}$ $Density = \frac{Mass}{Volume}$ $Pressure = \frac{Force}{Area}$	Including Speed, Density and Pressure.	Area and perimeter – 9.6 3D shapes – 10.11
	Error! Reference source not found.	Capture/Recapture method Stratified sampling		Ratio and proportion – 9.5 Probability – 10.8
11	Error! Reference source not found.	Substitution method	Algebraic solving Solving using graphical methods.	Simultaneous equations – 9.11 Linear graphs – 9.14 Quadratics – 10.6
11	Error! Reference source not found.	 Proof using 3 facts with reasons and a conclusion linked to either: SAS ASA 		Angles (parallel lines) – 9.4 Area and perimeter (shape properties) – 9.6 Circle theorems – 10.15

	• RHS			
Error! Reference source not found.	• SSS P(A or B) = P(A) + P(B), if mutually exclusive	Combined probabilities. Conditional probability using Venn Diagrams	Probability – 10.8 Quadratics – 10.6 (Algebraic fractions –	
Error! Reference source not found.	 Simplifying – factorise and cancel Adding/Subtracting – find a common denominator Multiplying and dividing – factorise and look to cross cancel when multiplying If the subject appears twice: Get all terms with the subject on one side and all others on the other Factorise the subject out using one bracket Divide by the bracket to get the subject on its own. 	Algebraic Fractions More complex Changing the subject	11.4.1) Fractions – 9.3 Algebra – 9.2 Equations – 9.11 Quadratics – 10.6 Probability (trees) – 11.3	
Error! Reference source not found.	Work with 2n, 2n+2 etc for consecutive even numbers and 2n-1, 2n+1 etc for consecutive odd numbers	Algebraic Proof	Algebra – 9.2 Quadratics – 10.6	
Error! Reference source not found.	 f(x) is another notation for y. f(2) is the y value when x = 2 f⁻¹(x) is the inverse function (use the method linked to changing the subject) Iteration is substituting a starting value into a formula to get a second value. The substitution is then repeated with this second value to perform a second iteration. 	Functions Iteration	Algebra (substitution) – 9.2 Algebraic fractions – 11.4.1	
Error! Reference source not found.	Upper and lower bounds Truncation Suitable degree of accuracy		Perimeter and area – 9.6 3D shapes – 10.11 Compound measure – 10.17	
Error! Reference source not found.	Observe vector triangle law To prove two lines are parallel show that the vectors are multiples of each other		Algebra – 9.2 Fractions – 9.3	

Error! Reference source not found.	$b^2 - 4ac >$ $b^2 - 4ac =$ $b^2 - 4ac <$ When sketch and ensure t point is in the	0 if there is 0 if there ar hing, label th he shape is o	1 root e no roo e roots a correct a	ts and y inf and the f	turning	Discriminant Solving by completing the square Sketching	Ratio – 9.5 Proof – 11.4.2 Quadratics – 10.6 Plotting graphs – 9.14
Error! Reference source not found.	$\frac{\sin(\theta)}{\cos(\theta)} = 0$			and example a formula for the formula	et values	Sin, cos, tan graphs Solving simple trig equations Exact trig values	Trigonometry – 9.12 Further trigonometry (sine rule ambiguous case) – 10.10
Error! Reference source not found.Transformation of graphs	Learn shapes					Cubic, reciprocal, exponential, circle graphs Graph transformations, including trig graphs	Simultaneous equations – 9.11 Plotting graphs – 9.14 Sketching Quadratics – 11.7
Error! Reference source not found.	Equation of a circle with origin as the centre is: $x^2 + y^2 = r^2$ Tangent is perpendicular to the radius					Equation of circle centred at origin Finding equation of tangents.	Pythagoras – 9.8 Trigonometry – 9.12 Linear graphs – 9.14 Circle theorems – 10.15